

GENETIC PARAMETERS FOR POST WEANING GROWTH OF NELLORE CATTLE USING POLINOMIALS AND TRIGONOMETRIC FUNCTIONS IN RANDOM REGRESSION MODELS

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ABSTRACT: Covariance functions and random regression models have been considered as an alternative for data adjustment, in sequence, stemming from the same animal along time and which presents a structured pattern of covariance. Aiming to evaluate the performance of random regression models based on the Legendre, modified Jacobi and trigonometric functions, data concerning the weights of Nelore breed animals were used from birth to the 800th day of life, in models that assumed direct additive and animal permanent environmental effects coefficients. The Schwarz Bayesian information criterion (BIC) led to the selection of the models Legendre of order six (ML6), Jacobi of order five (MJ5) and trigonometric of order six (MT6), the ML6 model presenting the lowest BIC. At the extremity of the interval, the MJ5 model presented lower variance of component estimates than those obtained through the ML6 model, however the estimates were in accordance to the medium part of the interval; while the estimates from the MT6 model were oscillating and different from those obtained through the other models. At the extremity of the interval, the heritability coefficient estimates (\hat{h}^2) obtained through the MJ5 model were lower than those obtained through the ML6 model, however, in the medium part of the interval, they were in accordance, remaining between 0.2 and 0.3. The values obtained through the MT6 model were different from those obtained through the other models, remaining between 0.35 and 0.40 on the first 285th days and then dropping to 0.01 on the 800th days of life. The means of the estimated growth curves started to distance from the data mean tendency from the 470th days on, and in this interval, the MT6 model was the most suitable.

Key words: additive variance, heritability, Jacobi, Legendre, longitudinal data

PARÂMETROS GENÉTICOS PARA CRESCIMENTO PÓS-DESMAME DE BOVINOS NELORE POR MEIO DE FUNÇÕES POLINOMIAIS E TRIGONOMÉTRICAS EM MODELOS DE REGRESSÃO ALEATÓRIA

RESUMO: O uso de funções de covariância e regressão aleatória tem sido considerado como uma alternativa para o ajuste de dados longitudinais com estrutura de covariância padrão, pois são mensurados no mesmo animal ao longo do tempo. Com objetivo de avaliar o desempenho dos modelos de regressão aleatória nas bases de funções de Legendre, de Jacobi modificada e as trigonométricas, os dados referentes aos pesos de animais da raça Nelore do nascimento aos 800 dias foram analisados com modelos que assumiram coeficientes de efeito aditivo direto e de ambiente permanente de animal. O critério de informação Bayesiano de Schwarz (BIC) conduziu a seleção dos modelos Legendre de ordem seis (ML6), Jacobi de ordem cinco (MJ5) e trigonométrica de ordem seis (MT6), dos quais, ML6 foi o modelo com o menor BIC. O modelo MJ5 apresentou estimativas de componentes de variância abaixo das estimativas obtidas pelo modelo ML6 nos extremos do intervalo e estimativas muito próximas no seu interior. Já as estimativas do modelo MT6 foram oscilantes e distintas das estimativas obtidas pelos demais modelos. Os coeficientes de herdabilidade (\hat{h}^2) estimados pelo modelo MJ5 ficaram abaixo das estimativas do modelo ML6 nos extremos do intervalo e no seu interior foram concordantes, entre 0,2 e 0,3. As estimativas obtidas pelo modelo MT6 se diferenciaram dos demais modelos, variando entre 0,35 e 0,40 aos 285 dias e diminuindo para 0,01 aos 800 dias de idade. As médias das curvas de crescimento estimadas se afastaram da tendência média dos dados a partir da idade 470 dias, e nesse intervalo a curva que mais se aproximou foi obtida pelo modelo MT6.

Palavras-chave: dados longitudinais, herdabilidade, Jacobi, Legendre, variância aditiva

INTRODUCTION

Covariance functions and random regression models have been considered as an alternative for the adjustment of data obtained in sequence from the same animal along time and which presents a structured pattern of covariance. This occurs due to the fact that phenotypic characteristics can be measured using same animal for a large number of times. Considering these unique characteristics, the results can be modeled using a continuous function based on the Legendre polynomials, especially after Kirkpatrick et al. (1990).

Polynomial regressions of 4th and 5th degrees presented better results for estimating genetic additive and maternal permanent environment effects using random regression to analyze data concerning growth measures of the Guzerath breed cattle (Scarpel, 2004). In addition, these polynomials present problems, producing variance components and genetic parameter estimates, at the interval extremities, which may not be reliable (Meyer, 2005). Those problems are due to the strong oscillation that the Legendre polynomials present at the extremities of the interval $[-1, 1]$.

Considering these problems, this study aims to identify possible differences in the random regression model adjustments when they are influenced by the Legendre polynomials, modified Jacobi and trigonometric functions, considering their application in data modeling related to body weight measures of the Nellore breed. The objectives were to compare fitted growth curves of animal weight post weaning; to investigate the behavior of the estimated random components of the curves; and to exam the behavior of the heritability coefficients of the curves.

MATERIAL AND METHODS

Data files consisted of 61,975 body weights measured on 20,543 animals which were kept grazing on tropical pastures, in Uberaba, Minas Gerais State, Brazil (19°45' S; 47°55' W), and in addition information from 26,275 pedigree Nellore animals was included. No animal was weighed more than six times, and each animal supplied at most, one measure within each of the following age intervals (in days): 1-69, 70-159, 160-

284, 285-454, 455-589 and 590-800 (brief description of the data is shown in Table 1). Weighing was performed between 1981 and 2002.

Data were organized in 670 contemporaneous groups (GC), considering the management group, the weaning (205 days), the year of birth and sex in each interval. Each GC consisted of weights of at least 18 animals, belonging to the offsprings of at least two different bulls. In addition, the data were classified into seven classes, named CIMP, according to the ages of dams at calving.

The purpose of this study was to consider random regression models that assume additive genetic and animal permanent environment effect coefficients as random factors. Therefore, all the data analysis was done using random regression models in which the orthonormal functions of the animal ages were considered as covariables of the random coefficients. Besides, a cubic regression using the Legendre polynomials (without the Legendre polynomial of degree zero) was added to the fixed effects of the model.

Data were disposed into six intervals, so that there were six random factors of possible maximum order of adjustment. The expressions of the functions belonging to the bases applied to this study were obtained through the Gram-Schmidt process of sequences of orthonormalization functions. A space coordinate X of all the functions within the domain $[-1, 1]$ and having the internal product (Kreyszig, 1978) given by $\langle x, y \rangle = \int_{-1}^1 x(t) y(t) dt$, $x, y \in X$, defines a Hilbert space, which is represented by $L^2[-1, 1]$.

Take the power functions, $\varphi_0(t) = 0$, $\varphi_1(t) = t$, $\varphi_2(t) = t^2$, ..., $\varphi_j(t) = t^j$, $t \in [-1, 1]$; take $\Delta(t) = (a + bt)^\alpha (a - bt)^\beta$, being $\alpha > -1$, $\beta > -1$; $a, b \in \mathbb{R}$ and $a \neq b$ if $a = 0$ or $b = 0$; the restrictions on α and β are needed to justify the integrability of Δ in the $[-1, 1]$ interval; if α and β assume positive integer values, Δ is a polynomial function and, therefore, x_0, x_1, x_2, \dots , in which $x_0(t) = \varphi_0(t)\Delta(t)$, $x_1 = \varphi_1(t)\Delta(t)$, $x_2 = \varphi_2(t)\Delta(t)$, ..., $x_j = \varphi_j(t)\Delta(t)$, $t \in [-1, 1]$ is a sequence of polynomials of weight Δ ; then, in order to orthonormalize the $(x_i)_{i \in \mathbb{N}}$ sequence, the Gram-smith process is once more used, considering the internal product defined in the $L^2[-1, 1]$ space. If $\alpha = \beta = 0$ in $\Delta(t)$, the result is a constant weight function, therefore, $\{x_0, x_1, \dots, x_j\}$ becomes a

Table 1 - Number of weighings (N), minimum, maximum and medium weights, and standard deviation of each age interval.

| Age | N | Weight | | | |
|---------|--------|----------------|---------|--------|--------------------|
| | | Minimum | Maximum | Medium | Standard Deviation |
| Days | | ----- kg ----- | | | |
| 285-454 | 12,325 | 95 | 441 | 213.22 | 42.28 |
| 455-589 | 9,892 | 104 | 546 | 292.76 | 52.25 |
| 590-800 | 9,757 | 165 | 653 | 347.37 | 62.90 |

sequence of power functions and its orthonormalization produces a base for the Legendre polynomial functions.

The base of modified Jacobi polynomial functions, $(\varpi_n)_{n \in N}$, can be obtained through the use of the Gram-Schmidt process in the orthonormalization of the sequence $(x_n)_{n \in N} = (\varphi_n \Delta)_{n \in N}$ being, $\Delta(t) = (1 - 1/2t)$.

The sequence $\{1, \cos(t), \sin(t), \cos(2t), \sin(2t), \dots, \cos(kt), \sin(kt)\}$ orthonormalized by the Gram-Schmidt process, with the internal product given by $\langle x, y \rangle = \int_{-1}^1 x(t) y(t) dt$, $x, y \in X$, generates the base of the trigonometric functions with the domain $[0, 2\pi]$. The following random regression model (Kirkpatrick et al., 1990; Meyer, 1998) was used:

$$y_{ij} = F + \sum_{m=1}^3 \beta_m \phi_m(t_{ij}^*) + \sum_{m=0}^{k_a-1} \alpha_{im} \psi_m(t_{ij}^*) + \sum_{m=0}^{k_p-1} \gamma_{im} \psi_m(t_{ij}^*) + \varepsilon_{ij}$$

in which, y_{ij} is the i^{th} animal weight at its j^{th} age; F represents part of the fixed effects; t_{ij}^* is the j^{th} age for the i^{th} animal, standardized for the domain interval associated to the base of the orthonormal functions used in the adjustment; $\phi_m(t_{ij}^*)$ is the m^{th} Legendre polynomial evaluated in t_{ij}^* ; β_m is the m^{th} regression coefficient of the fixed effect of the weight at the age; α_{im} and γ_{im} are the m^{th} random regression coefficients for the direct additive genetic and permanent environment effects, respectively, for the i^{th} animal; $\psi_m(t_{ij}^*)$ represents a function of the Legendre or Modified Jacobi orthonormal base or of the trigonometric functions evaluated in t_{ij}^* ; $k_a = k_p \in \{2, 3, 4, 5, 6\}$ is the order of adjustment of the orthonormal functions and ε_{ij} is the random error.

The F term of the model includes the fixed effects of GC and CIMP. The random regression model in its matrix form is:

$$y = Xb + Z^* a + Z_D^* p + \varepsilon,$$

in which, $y = [y_1, y_2, \dots, y_{20,543}]$ is the vector corresponding to the weight of the 20,543 animals. The weight of individuals was disposed, always, after the weight of their ancestors and in crescent order of age at the time of the weighing. The incidence matrix for the models fixed effects is represented by X , b is the fixed effect parameter vector given by $b = [CIMP_1, CIMP_2, \dots, CIMP_7, GC_1, GC_2, \dots, GC_{670}, \beta_1, \beta_2, \beta_3]$.

The vectors $a = [a_1, a_2, \dots, a_{20,543}]$ and $p = [p_1, p_2, \dots, p_{20,543}]$ represent the random regression models for additive genetic and animal permanent environmental effects, respectively, and ε is the residual vector.

The matrixes Z^* and Z_D^* are the incidence matrixes of the random factors and their elements are null, they are the images of functions that belong to one of the bases of the orthonormal functions.

If $K_A = \text{cov}(a, a)$ and $K_p = \text{cov}(p, p)$, then K_A and K_p are called coefficient matrixes for the additive genetic and animal permanent environment covariance functions, G_0 and C_0 , respectively.

It was assumed that the fixed part of the model takes into account the systematic effects of age, which means that $a \sim N(0, K_A \otimes A)$ and $p \sim N(0, K_p \otimes I_{20,543})$, and that $\text{cov}(a, p) = 0$. It was also assumed that $V(\varepsilon) = R$, which means that the expression of the restricted likelihood function logarithm for the random regression model (Meyer, 1989, 1998) is given by:

$$-2L(\theta) = \text{const} + N_A \ln(|K_A|) + K_A \ln(|A|) + N_D \ln(|K_p|) + \ln(|R|) + \ln(|C^*|) + y^T P y,$$

in which, θ is the vector formed by the parameters that are presented as the matrixes K_A and K_p elements, N_A is the total number of animals in the analysis, N_D is the number of animals that provided the data, A is the kinship matrix, C^* is the mixed model equations coefficients matrix and $P = V^{-1} - V^{-1} X(X^T V^{-1} X)^{-1} X^T V^{-1}$, being $\text{Var}(y) = V$.

The WOMBAT device (Meyer, 2006) was used for the data analysis. Among the many available algorithms of this device, the PX-AI algorithm was chosen, because, it combines the PX (parameter expanded) method, which is a variation of the EM (expectation-maximization) algorithm, with the AI (average information) algorithm (Meyer, 1997).

The assessment of the best fitted model is given in relation to the maximum likelihood ratio test (LRT), the Akaike information criterion (AIC) and the Schwarz Bayesian criterion (BIC). The AIC and BIC criteria apply penalties for the number of estimated parameters.

For each base of orthonormal functions, Legendre, modified Jacobi and trigonometric, five random regression models were analyzed, assuming heterogeneity of the residual variances in the six age sub-intervals.

To simplify the presentation of the results, the random regression models were identified through MBm, in which, M stands for model, B stands for the base of orthonormal functions used in the analysis, which can be L = Legendre, J = Jacobi and T = Trigonometric; $m \in \{2, 3, 4, 5, 6\}$ represents the adjustment order of the random coefficients assumed by the model.

RESULTS AND DISCUSSION

There were differences, according to the LRT (Table 2), between the likelihood function logarithm values χ^2_{12} in the three bases of orthonormal functions, once all the LRT calculated values were superior to the critical value of the distribution which is approximately 26.2 ($p = 0.01$), which indicates that the most

Table 2 - Number of parameters (p), value of the likelihood function logarithm (L), likelihood ratio test (LRT), Akaike information criterion (AIC) and Schwartz Bayesian information criterion (BIC) for the fitted random regression models with different orders for the additive genetic and animal permanent environment effects.

| Model ¹ | p | L | LRT | AIC | BIC |
|--------------------|----|--------------|-------------------|-------------|-------------|
| Legendre | | | | | |
| (1) ML2 | 12 | -203,529.762 | - | 407,083.524 | 407,191.806 |
| (2) ML3 | 18 | -201,796.064 | (2 - 1) 1,733.698 | 403,628.128 | 403,790.552 |
| (3) ML4 | 26 | -200,923.027 | (3 - 2) 873.037 | 401,898.054 | 402,132.664 |
| (4) ML5 | 36 | -200,730.423 | (4 - 3) 192.604 | 401,532.846 | 401,857.690 |
| (5) ML6 | 48 | -200,618.053 | (5 - 4) 112.370 | 401,332.106 | 401,765.232 |
| Modified Jacobi | | | | | |
| (1) MJ2 | 12 | -202,771.126 | - | 405,566.252 | 405,674.534 |
| (2) MJ3 | 18 | -201,970.384 | (2 - 1) 800.742 | 403,976.768 | 404,139.190 |
| (3) MJ4 | 26 | -200,983.466 | (3 - 2) 986.918 | 402,018.932 | 402,253.542 |
| (4) MJ5 | 36 | -200,700.086 | (4 - 3) 283.380 | 401,472.172 | 401,797.018 |
| (5) MJ6 | 48 | -200,654.785 | (5 - 4) 45.301 | 401,405.570 | 401,838.698 |
| Trigonometric | | | | | |
| (1) MT2 | 12 | -206,616.633 | - | 413,257.266 | 413,365.548 |
| (2) MT3 | 18 | -205,649.850 | (2 - 1) 966.783 | 411,335.700 | 411,498.122 |
| (3) MT4 | 26 | -202,973.719 | (3 - 2) 2,676.131 | 405,999.438 | 406,234.050 |
| (4) MT5 | 36 | -202,768.186 | (4 - 3) 205.533 | 405,608.372 | 405,933.218 |
| (5) MT6 | 48 | -201,806.617 | (5 - 4) 961.569 | 403,709.234 | 404,142.360 |

¹ML6 = model fitted through Legendre functions of order six; MJ6= model fitted through modified Jacobi functions of order six; MT6 = model fitted through trigonometric function of order six

suitable situation for the data in each of the base of orthonormal functions occurred in the models with 48 parameters. The ML6 and MT6 models were selected according to the AIC and BIC criteria. For the base of modified Jacobi functions, the AIC criterion, led to the selection of the MJ6 model, however the BIC criterion led to the selection of the MJ5 model. In this case, considering the parsimony, because of the lowest number of estimated parameters, the MJ5 model was chosen.

Among the ML6, MJ5 and MT6 models, the log values (L) and the AIC and BIC criteria indicated that the ML6 model was the one that was best adjusted to the data.

The direct additive genetic variance curves (Figure 1) presented a very strong growth tendency up to the 600 days, reaching their peak and then plunging in the last subinterval of the age domain. The curves estimated through the ML6 and MJ5 models became more apart from each other at the beginning and end of the age interval and the curve estimated through the MT6 model presented a particularly strong oscillation as compared to the other curves. Probably the presence of data concerning animals at ages higher than 650 days in the ML6 and MJ6 models could have influenced the variance component estimates, and as a consequence, the h^2 estimates.

The animal permanent environment variance curves (Figure 2) reached the peak between the second from last (454 – 589) and last (589 – 800) sub-intervals of the age domain and had then a strong decrease near the top extremity of this interval, which indicates that the environmental effect prevailed over the additive genetic effect. The curves estimated through the ML6 and MJ5 models were distant from each other only at the end of the age interval. The curve estimated through the MT6 model presented strong oscillations being, once more, different from the other curves.

As a hypothesis, the variances of the residuals were considered as constant in each subinterval, which explains the discontinuity (Figure 3). Accordingly, it can be verified that the curves estimated through ML6 and MJ5 were very close to each other, while the curve estimated through the MT6 model was different from the other curves, mainly in the second and sixth sub-intervals of the age domain.

The variance components and heritability coefficient estimates for the age vector $t = [365, 550, 730, 800]$ obtained through the models ML6, MJ5 and MT6 are summarized in Table 3. The variances and heritability coefficient estimated values, obtained through the ML6 and MJ5 models, were very close

Table 3 - Variance components and heritability coefficients estimates for different ages obtained through the Legendre order six (ML6), modified Jacobi order five (MJ5) and trigonometric order six (MT6) models.

| Age | ML6 | | | | MJ5 | | | | MT6 | | | |
|-----|--------------------|-----------------------|--------------------|-------------|--------------------|-----------------------|--------------------|-------------|--------------------|-----------------------|--------------------|-------------|
| | $\hat{\sigma}_a^2$ | $\hat{\sigma}_{pe}^2$ | $\hat{\sigma}_e^2$ | \hat{h}^2 | $\hat{\sigma}_a^2$ | $\hat{\sigma}_{pe}^2$ | $\hat{\sigma}_e^2$ | \hat{h}^2 | $\hat{\sigma}_a^2$ | $\hat{\sigma}_{pe}^2$ | $\hat{\sigma}_e^2$ | \hat{h}^2 |
| 365 | 330.3 | 410.3 | 194.8 | 0.35 | 354.8 | 462.2 | 195.6 | 0.35 | 318.1 | 509.9 | 186.3 | 0.31 |
| 550 | 441.6 | 850.0 | 126.5 | 0.31 | 462.2 | 890.8 | 123.6 | 0.31 | 405.9 | 881.6 | 127.2 | 0.29 |
| 730 | 578.9 | 837.3 | 341.0 | 0.31 | 538.5 | 756.4 | 353.7 | 0.33 | 156.1 | 354.9 | 576.5 | 0.14 |
| 800 | 836.6 | 681.4 | 341.0 | 0.45 | 483.6 | 481.7 | 353.7 | 0.37 | 4.6 | 6.4 | 576.5 | 0.01 |

$\hat{\sigma}_a^2$ = additive direct genetic variance; $\hat{\sigma}_{pe}^2$ = animal permanent environment effect variance; $\hat{\sigma}_e^2$ = residual variance; \hat{h}^2 = heritability for direct effect;

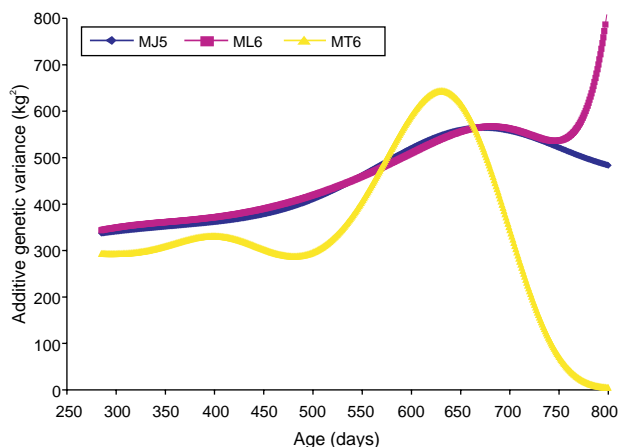


Figure 1 - Direct additive genetic variance curves estimated by the Legendre order six (ML6), modified Jacobi order five (MJ5) and trigonometric order six (MT6) models.

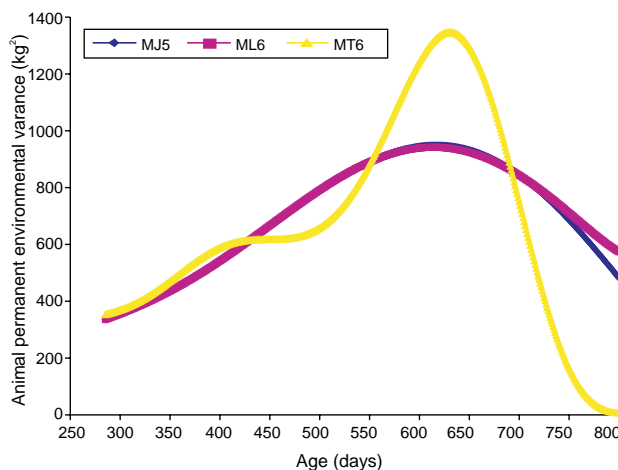


Figure 2 - Animal permanent environment variance curves estimated by the Legendre order six (ML6), modified Jacobi order five (MJ5) and trigonometric order six (MT6) models.

at the ages 365, 550 and 730 days, and presented huge differences at birth and at 800 days, the values estimated through the MJ5 model being smaller, which indicates that the random regression model under the influence of the modified Jacobi functions produces smoother curves at the extremities of the age interval (Figure 4), and that the random regression model

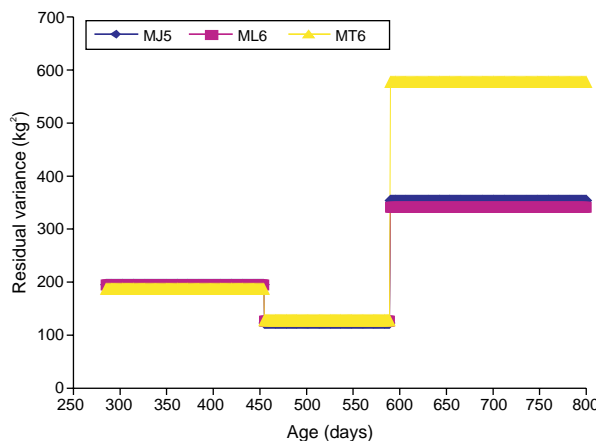


Figure 3 - Residual variance curves estimated by the Legendre order six (ML6), modified Jacobi order five (MJ5) and trigonometric order six (MT6) models.

theory can contribute to solving problems associated to models that use the Legendre polynomials (Meyer, 2005).

For the values estimated through the MT6 model an oscillatory tendency was again verified, and that also the estimates for the ages 730 and 800 days were very low when compared to the heritability coefficients estimated through the ML6 and MJ5 models.

The models under the influence of these bases, the Legendre and modified Jacobi functions, presented similar results in the center of the domain, when compared to the variability of the Legendre functions at the extremities.

A univariate model for data composed of Nellore cattle weights (Figueiredo, 2001), obtained at the same farm, presented 0.29 as the h^2 estimate at the yearling stage. These values are not too distant from the heritability estimates obtained by the ML6 and MJ5 models at the yearling stage. Most recently, also with the same herd used in this study (Figueiredo et al., 2005), the h^2 estimates were 0.34 and 0.36 for the weight traits at the yearling stage and at 18 months, respectively. At yearling, the estimate was very close to the ones obtained through the ML6 and MJ5 models.

Also an univariate analysis to study data collected from Nellore cattle (Oliveira, 2005), with a model considered as direct additive genetic, direct maternal genetic and maternal permanent environment effects, resulted in h^2 estimates as follows: 0.36; for the weight at yearling, which was in accordance to the h^2 values estimated through the ML6 and MJ5 models at the yearling stage and at 18 months.

Also working with random regression models with classes of four days in the analysis of Nellore cattle weight, from birth to 630 days, Albuquerque & Meyer (2001) obtained h^2 estimates between 0.2 and 0.4 from birth to 450 days, which were in disagreement with the h^2 values estimated through the models of this study, which showed h^2 values higher than 0.40 from birth to 284 days, probably due to the absence of the

maternal effect in the models. In addition, Albuquerque & Meyer (2001) and Santoro et al. (2005), obtained h^2 estimates between 0.4 and 0.6 for the interval of age ranging from 450 to 630 days, in disagreement to the h^2 values estimated by this study, as well.

The ML6, MJ5 and MT6 allowed the estimation of the growth curve for each of the animals involved in the analysis. The graphic representation of all the growth curves estimated through the ML6, MJ5 and MT6 models is not easy to interpret, for this reason the curves obtained through all the growth curves fitted through each model are presented in Figure 5, together with the data means in each point in the interval [285, 800].

Finally, the absence of the maternal effect in the model should be considered. This may promote changes in the estimates, mainly up to the yearling stage; however, it should not jeopardize the analysis to express the methodological differences.

CONCLUSIONS

The differences in the variance curves constitute evidence to the nature of the functions belonging to the bases of the orthonormal functions, indicating that these different bases have influence on the variance component estimation, and as a consequence, influence on the genetic parameter estimation.

The Legendre and modified Jacobi functions were of polynomial nature, but they show differences at the extremities due to the smaller variability of the modified Jacobi functions at the beginning and end of the domain interval.

The trigonometric functions presented oscillatory variance curves through all their domain, which is undesirable.

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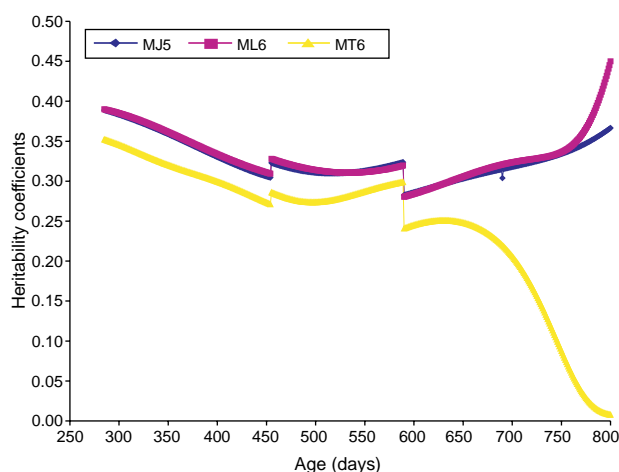


Figure 4 - Heritability coefficient curves at different ages estimated by the Legendre order six (ML6), modified Jacobi order five (MJ5) and trigonometric order six (MT6) models.

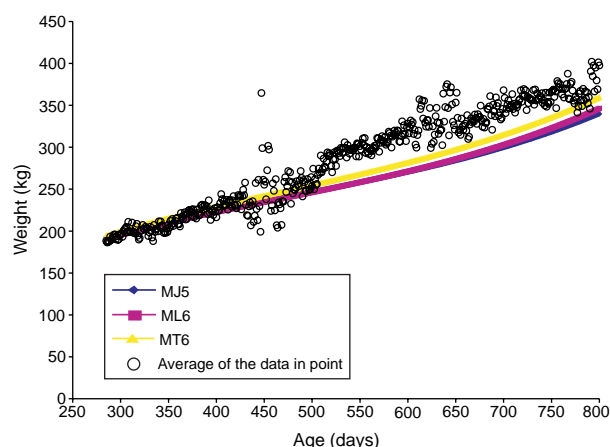


Figure 5 - Means of the weight curves estimated by the Legendre order six (ML6), modified Jacobi order five (MJ5) and trigonometric order six (MT6) models, in relation to the average tendency of the data at each point of the age interval.

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